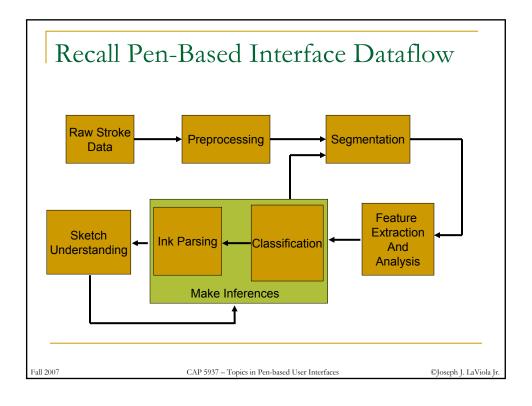
Ink Parsing in Sketch-Based Interfaces

Lecture #10: Ink Parsing Joseph J. LaViola Jr. Fall 2007

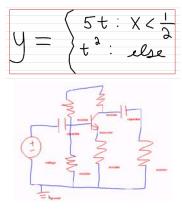
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Sketch Parsing

- Often recognition of strokes is insufficient
 - except for gestures
- Require an understanding of spatial relationships
 - good examples are mathematical expressions
- Higher level classifications
 - is it a word or a drawing?



www.engr.ucr.edu/~stahov/research/acsparc.htm

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Approaches to Sketch Parsing

- Top down vs. bottom up
- Focus on mathematical expressions
 - 2D (coordinate) grammars
 - graph rewriting
 - useful for other types of parsing as well (diagrams, tables, lists, etc...)
 - projection profile cutting
 - procedurally coded syntax rules
 - stochastic grammars
- Other parsing approaches
 - conditional random fields
 - statistical visual languages
 - many others

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2D Grammars

- Grammar + spatial relationship rules
 - useful if a well defined syntax exists
 - looks for key symbols
- One Approach Box Grammar
 - divide input into distinct areas based on symbol found



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Graph Rewriting

- Expressions represented as nodes and arcs
- Rewrite rules applied to graph to reduce it progressively
 - rules are also subgraphs
 - graph reduced to single node representing expression

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Graph Rewriting Example (Blostein and Grbavec 1996)

- Build
 - add edges between symbols (above, below, left, superscript, subscript)
- Constrain
 - Apply knowledge of notational conventions
 - remove contradictory associations
 - disambiguate horizontal lines
 - disambiguate dots
 - disambiguate diagonal associations
- Rank
 - Use information about operator precedence to group symbols into subexpressions
- Incorporate
 - Interpret subexpressions

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Projection Profile Cutting

- Used primarily in document analysis
- Uses horizontal and vertical projections of expression onto x and y axis
 - subdivides expression recursively
- Problem with expressions where symbols are close together (no white space)

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Procedurally Coded Syntax Rules

- Observations about domain coded programmatically
 similar to rule based approach for recognition
- Sample rule for horizontal line

A length threshold of 20 pixels is used to classify a horizontal line as a short or long bar.

If it is a long bar and has symbols above and below, it is treated as a division.

If there are no symbols above, it is treated as a boolean negation.

If a short bar has no symbols above or below, it is treated as minus sign.

If it has symbols above or below, the combination symbols such as =, \leq , and \geq are formed.

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Stochastic Grammars

- Used to deal with noisy data and spatial ambiguities
- Probabilities associated with each production rule
- For any sequence in a given parse probability can be calculated
- Requires training

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MathPad² Parsing Approach

- Uses 2D coordinate grammar approach with some syntax rules
- Basic approach
 - preprocessing step (for functions)
 - sort list of symbols
 - parse functions use grammar
 - process functions handle spatial relationship testing
 - intermixed with parse functions

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Grammar (1)

```
<math_formula>
                ::= <equation> | <expression>
<equation>
               ::= <expression> <relational_op> <expression> |
<cond_expression> ::= ''{',' <cond_statement>
<cond_statement> ::= ''if'' <expression> '':'' <logic_expression>
               {''elseif'' <expression> '':'' <logic_expression> }
                  <expression> '': else''
<logic_expression> ::= <equation> <logical_op> <logic_expression> | <equation>
<logic_op> ::= ''and'' | ''or''
               ::= <term> ''+'' <expression>
<expression>
                   <term> ('-') <expression>
                   <term> ''^'' <expression> |
                   <term>
               ::= <factor> ''*', <term>
<term>
                   "((" <expression> ")" |
                   <factor>
<factor>
                ::= <sub_expression> ''/', <factor> |
                   <sub_expression>
<sub_expression>
               ::= <integral> | <derivative> | <summation> |
                   <function> | <terminal>
```

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Grammar (2)

```
<integral>
<derivative>
             ::= ''sum('' <expression> '')'' |
<summation>
               "('sum('('<expression>'(',')' <expression>'(',')' <expression>'(',')'
             <function>
<func_name>
             ::= <variable> | <number>
<terminal>
             <variable>
             <number>
             ::= <sign> <unsigned_int> | <unsigned_int>
<integer>
<unsigned_int>
             ::= <digit> <unsigned_int> | <digit>
<sign>
             ::= '(+) | '(-)
             ::= [0-9]
<digit>
             ::= [a-z] | [A-Z] | [alpha-zeta]
<letter>
```

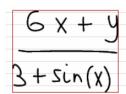
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Parse functions

- High level parse
- Expression parse
- Sub-expression parse
- Symbol specific parsing
 - square root parse
 - integration parse
 - summation parse
 - fraction parse
- Factor parse
- Term parse





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Process functions

- Provide parse functions important info
- Deal with spatial relationships
 - implicit operators
 - fractions and square roots
 - summations , derivatives, integrals
 - Conditionals

$$X(t+h) = \begin{cases} l-r : X(t) > (l-r) \\ r : X(t) < r \\ X(t) + Vh : else \end{cases}$$

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Reducing parsing decisions

- Use application to reduce decisions
- Implicit operators (no numbers have subscripts)
- Correct trig functions 5in -> sin
- Functions of time f(+) -> f(t)

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Readings

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