

Formulas

$$\int_a^b \delta(t-T)g(t)dt = \begin{cases} g(T), & a < T < b \\ 0, & \text{else} \end{cases}$$

$$f(t) = a_0 + \sum_{n=1}^{\infty} (a_n \cos n\omega_0 t + b_n \sin n\omega_0 t),$$

$$a_n = \frac{2}{T} \int_T f(t) \cos n\omega_0 t dt$$

$$b_n = \frac{2}{T} \int_T f(t) \sin n\omega_0 t dt$$

$n=1, 2, \dots$

$$f(t) = c_0 + \sum_{n=1}^{\infty} c_n \cos(n\omega_0 t + \theta_n)$$

$$\omega_0 = \frac{2\pi}{T}$$

$$f(t) = \sum_{n=-\infty}^{\infty} D_n e^{jn\omega_0 t},$$

$$a_0 = c_0 = \frac{1}{T} \int_T f(t) dt$$

$$D_n = \frac{1}{T} \int_T f(t) e^{-jn\omega_0 t} dt, \quad n=0, \pm 1, \pm 2, \dots$$

$$2D_n = c_n e^{j\theta_n} = a_n - jb_n$$

$$e^{\pm j\theta} = \cos \theta \pm j \sin \theta; \quad \cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$P = \frac{1}{T} \int_T |f^2(t)| dt, \quad [f(t) \text{ periodic}]$$

$$E = \int_{-\infty}^{\infty} |f^2(t)| dt$$

Indefinite Integrals

$$\int u dv = uv - \int v du$$

$$\int f(x)g'(x) dx = f(x)g(x) - \int f'(x)g(x) dx$$

$$\int \sin ax dx = -\frac{1}{a} \cos ax \quad \int \cos ax dx = \frac{1}{a} \sin ax$$

$$\int \sin^2 ax dx = \frac{x}{2} - \frac{\sin 2ax}{4a} \quad \int \cos^2 ax dx = \frac{x}{2} + \frac{\sin 2ax}{4a}$$

$$\int x \sin ax dx = \frac{1}{a^2} (\sin ax - ax \cos ax)$$

$$\int x \cos ax dx = \frac{1}{a^2} (\cos ax + ax \sin ax)$$

$$\int x^2 \sin ax dx = \frac{1}{a^3} (2ax \sin ax + 2 \cos ax - a^2 x^2 \cos ax)$$

$$\int x^2 \cos ax dx = \frac{1}{a^3} (2ax \cos ax - 2 \sin ax + a^2 x^2 \sin ax)$$

$$\int \sin ax \sin bx dx = \frac{\sin(a-b)x}{2(a-b)} - \frac{\sin(a+b)x}{2(a+b)} \quad a^2 \neq b^2$$

$$\int \sin ax \cos bx dx = -\left[\frac{\cos(a-b)x}{2(a-b)} + \frac{\cos(a+b)x}{2(a+b)} \right] \quad a^2 \neq b^2$$

$$\int \cos ax \cos bx dx = \frac{\sin(a-b)x}{2(a-b)} + \frac{\sin(a+b)x}{2(a+b)} \quad a^2 \neq b^2$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax}$$

$$\int x e^{ax} dx = \frac{e^{ax}}{a^2} (ax - 1)$$

$$\int x^2 e^{ax} dx = \frac{e^{ax}}{a^3} (a^2 x^2 - 2ax + 2)$$

$$\int e^{ax} \sin bx dx = \frac{e^{ax}}{a^2 + b^2} (a \sin bx - b \cos bx)$$

$$\int e^{ax} \cos bx dx = \frac{e^{ax}}{a^2 + b^2} (a \cos bx + b \sin bx)$$

$$\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}$$

$$\int \frac{x}{x^2 + a^2} dx = \frac{1}{2} \ln(x^2 + a^2)$$

$$f_{IFM} = 455 \text{ kHz}; f_{IF} = 10.7 \text{ MHz}$$

$$\phi_{FM}(t) = A \cos[\omega_c t + k_f \int_{-\infty}^t m(\alpha) d\alpha] *$$

$$\phi_{PM}(t) = A \cos[\omega_c t + k_p m(t)]$$

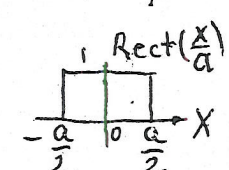
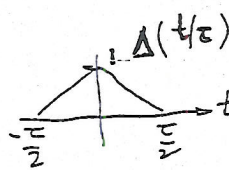
$$\text{FM or PM bandwidth} = 2(\Delta\omega + \omega_m) \frac{\text{Rad}}{\text{sec}} = 2\omega_m(\beta + 1) \frac{\text{Rad}}{\text{sec}} \cdot \omega_m = \text{message bandwidth} \left(\frac{\text{Rad}}{\text{sec}} \right)$$

$$\phi_{AM}(t) = [A + m(t)] \cos \omega_c t$$

$$\phi_{SSB}(t) = m(t) \cos \omega_c t \mp m_h(t) \sin \omega_c t$$

$$\text{Sampling period } T \leq \frac{1}{2B}$$

	$g(t)$	$G(\omega)$	
1	$e^{-at} u(t)$	$\frac{1}{a + j\omega}$	$a > 0$
2	$e^{at} u(-t)$	$\frac{1}{a - j\omega}$	$a > 0$
3	e^{-at}	$\frac{2a}{a^2 + \omega^2}$	$a > 0$
4	$t e^{-at} u(t)$	$\frac{1}{(a + j\omega)^2}$	$a > 0$
5	$t^n e^{-at} u(t)$	$\frac{n!}{(a + j\omega)^{n+1}}$	$a > 0$
6	$\delta(t)$	1	
7	1	$2\pi \delta(\omega)$	
8	$e^{j\omega_0 t}$	$2\pi \delta(\omega - \omega_0)$	
9	$\cos \omega_0 t$	$\pi [\delta(\omega - \omega_0) + \delta(\omega + \omega_0)]$	
10	$\sin \omega_0 t$	$j\pi [\delta(\omega + \omega_0) - \delta(\omega - \omega_0)]$	
11	$u(t)$	$\pi \delta(\omega) + \frac{1}{j\omega}$	
12	$\text{sgn } t$	$\frac{2}{j\omega}$	
13	$\cos \omega_0 t u(t)$	$\frac{\pi}{2} [\delta(\omega - \omega_0) + \delta(\omega + \omega_0)] + \frac{j\omega}{\omega_0^2 - \omega^2}$	
14	$\sin \omega_0 t u(t)$	$\frac{\pi}{2j} [\delta(\omega - \omega_0) - \delta(\omega + \omega_0)] + \frac{\omega_0}{\omega_0^2 - \omega^2}$	
15	$e^{-at} \sin \omega_0 t u(t)$	$\frac{\omega_0}{(a + j\omega)^2 + \omega_0^2}$	$a > 0$
16	$e^{-at} \cos \omega_0 t u(t)$	$\frac{a + j\omega}{(a + j\omega)^2 + \omega_0^2}$	$a > 0$
17	$\text{rect}\left(\frac{t}{\tau}\right)$	$\tau \text{sinc}\left(\frac{\omega\tau}{2}\right)$	
18	$\frac{W}{\pi} \text{sinc}(Wt)$	$\text{rect}\left(\frac{\omega}{2W}\right)$	
19	$\Delta\left(\frac{t}{\tau}\right)$	$\frac{\tau}{2} \text{sinc}^2\left(\frac{\omega\tau}{4}\right)$	
20	$\frac{W}{2\pi} \text{sinc}^2\left(\frac{Wt}{2}\right)$	$\Delta\left(\frac{\omega}{2W}\right)$	
21	$\sum_{n=-\infty}^{\infty} \delta(t - nT)$	$\omega_0 \sum_{n=-\infty}^{\infty} \delta(\omega - n\omega_0)$	$\omega_0 = \frac{2\pi}{T}$
22	$e^{-t^2/2\sigma^2}$	$\sigma\sqrt{2\pi} e^{-\omega^2/2\sigma^2}$	



Fourier Transform Operations

Operation	$g(t)$	$G(\omega)$
Addition	$g_1(t) + g_2(t)$	$G_1(\omega) + G_2(\omega)$
Scalar multiplication	$k g(t)$	$k G(\omega)$
Symmetry	$G(t)$	$2\pi g(-\omega)$
Scaling	$g(at)$	$\frac{1}{ a } G\left(\frac{\omega}{a}\right)$
Time shift	$g(t - t_0)$	$G(\omega) e^{-j\omega t_0}$
Frequency shift	$g(t) e^{j\omega_0 t}$	$G(\omega - \omega_0)$
Time convolution	$g_1(t) * g_2(t)$	$G_1(\omega) G_2(\omega)$
Frequency convolution	$g_1(t) g_2(t)$	$\frac{1}{2\pi} G_1(\omega) * G_2(\omega)$
Time differentiation	$\frac{d^n g}{dt^n}$	$(j\omega)^n G(\omega)$
Time integration	$\int_{-\infty}^t g(x) dx$	$\frac{G(\omega)}{j\omega} + \pi G(0) \delta(\omega)$

* take the value of the integral at $\omega = 0$ to be > 0