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# Energy-Efficient Discrete Signal Processing with Field Programmable Analog Arrays (FPAAs)

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# Why Convolution?

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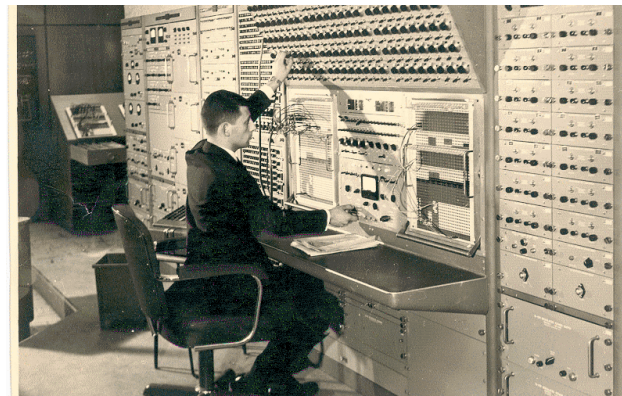
- Large-Scale Convolution is the Computing Engine of many CV, AI, and DSP application
  - Image Classification, Edge Detection, ...
  - Deep Learning: Convolutional 3D-Network, ...
  - Video Object Recognition, ...
- But, Computationally Intensive
  - Energy Consumption High
  - Fault Tolerance Low
  - Time Complexity  $O(n^2)$  or  $O(n \lg(n))$  even with complicated FFT-based method

# Analog Computing

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- Digital Computing vs. Analog Computing

- Energy Efficiency
- Performance
- Hardware Effectiveness

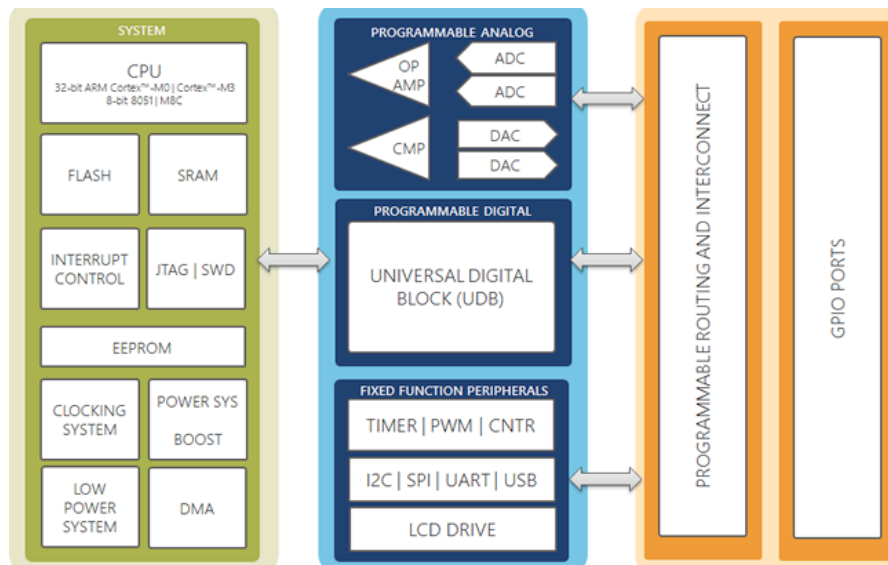


- Analog Computing is HARD!

- Flexible and Effective Prototyping Platform is Lacking
  - Resource Constraints
  - Noise Sensitivity
  - No Unified Computing Framework for Complicated Task
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# What about Reconfigurable Analog Computing?

Limited Resource Type: No Universal Logic Gate Set, No LUT ....



No Straightforward Design Framework: No Logic Synthesis + Technology Packing ....

Very Sensitive to Noise and Design Parameters: The General Nature of Analog Computing ...

# Our Idea

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Probabilistic-Base Computing

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Large-Scale Convolution

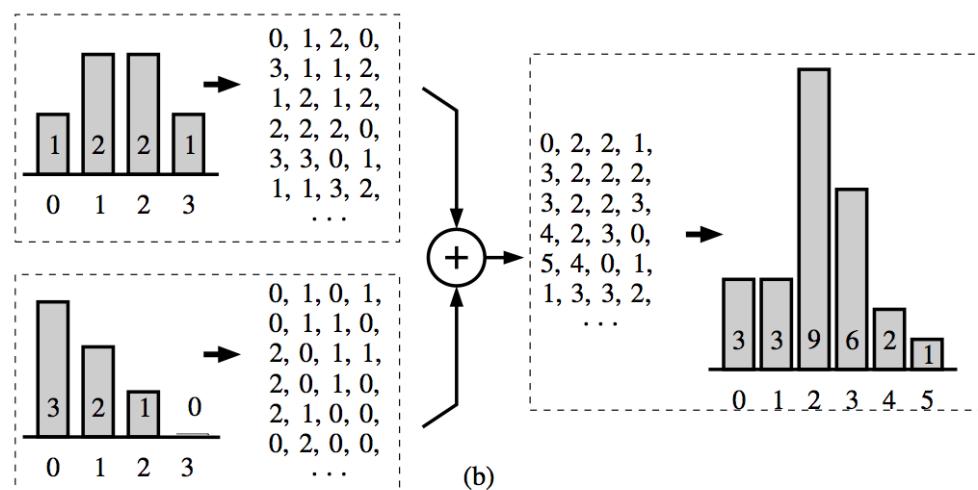
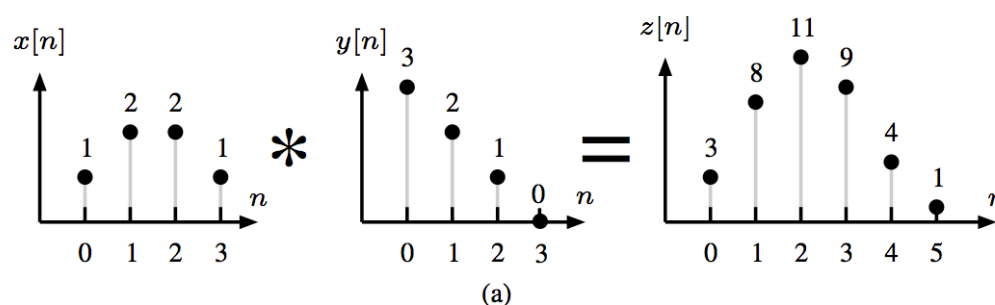
Field-Programmable Analog Array

- Prototyping
- Resource Constraints
- Noise Sensitivity
- No Unified Computing Framework

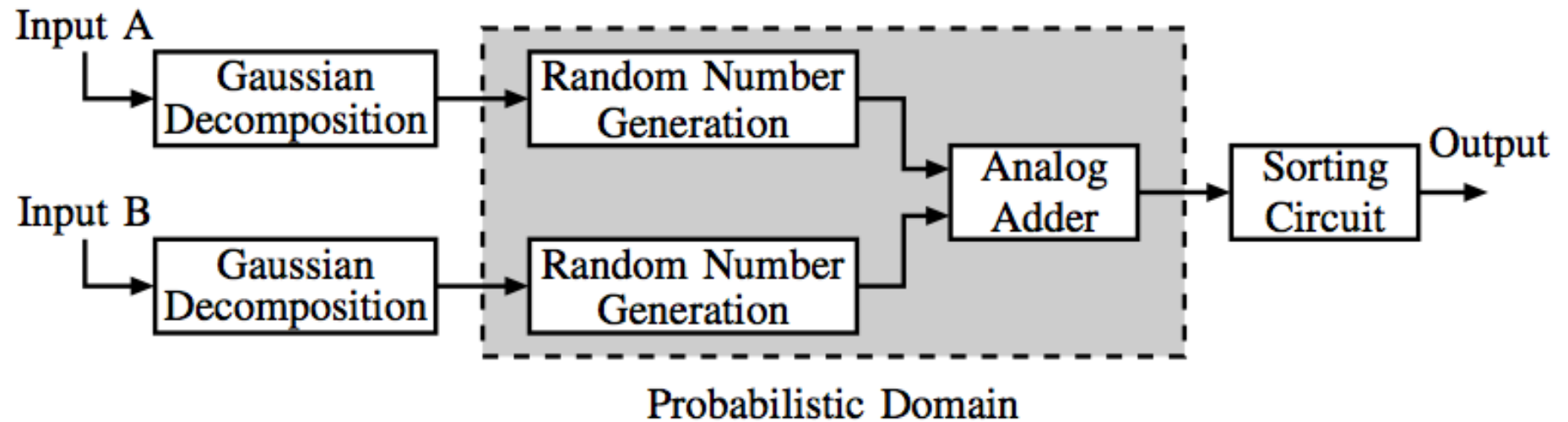
# Probabilistic Method for Convolution

- Probabilistic Convolution Theorem<sub>z</sub>

$$f_Z(z) = f_{X+Y}(z) = P(Z = z) = \sum_{x=0}^z f_X(x) f_Y(z - x)$$

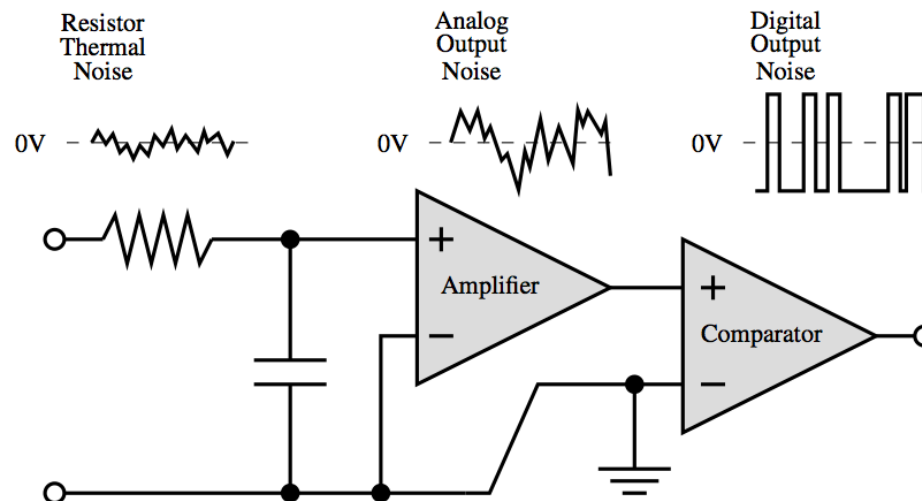


# Overall Algorithm Flow



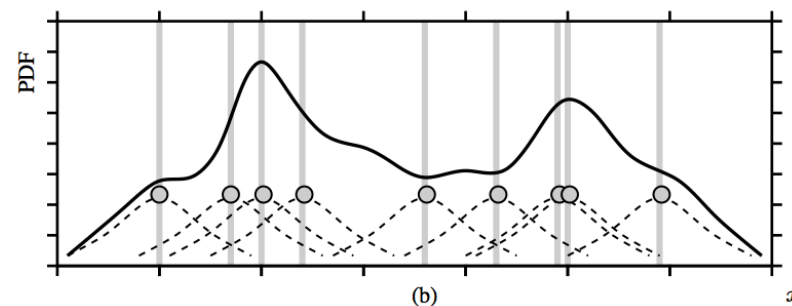
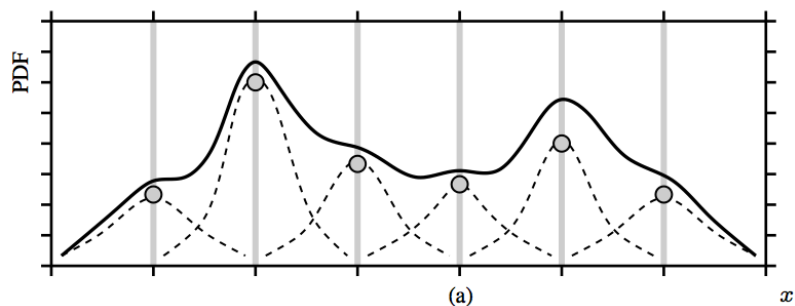
# Input $\rightarrow$ PDF $\rightarrow$ Random Samples

- Direct Implementation too costly
- Objective: Given any form of PDF, efficiently generating a large ensemble of random samples
- Method:
  - Gaussian noise source + Gaussian Decomposition
- Gaussian Noise Random Sample Generator

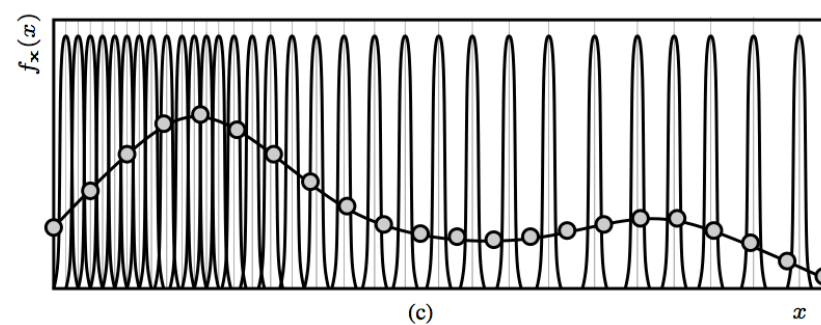
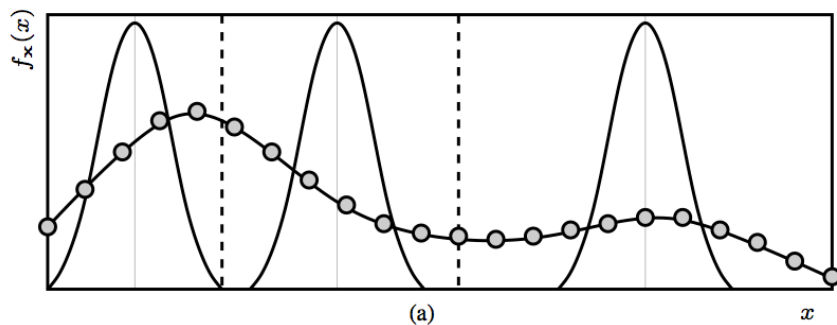




# Gaussian Decomposition: Concept

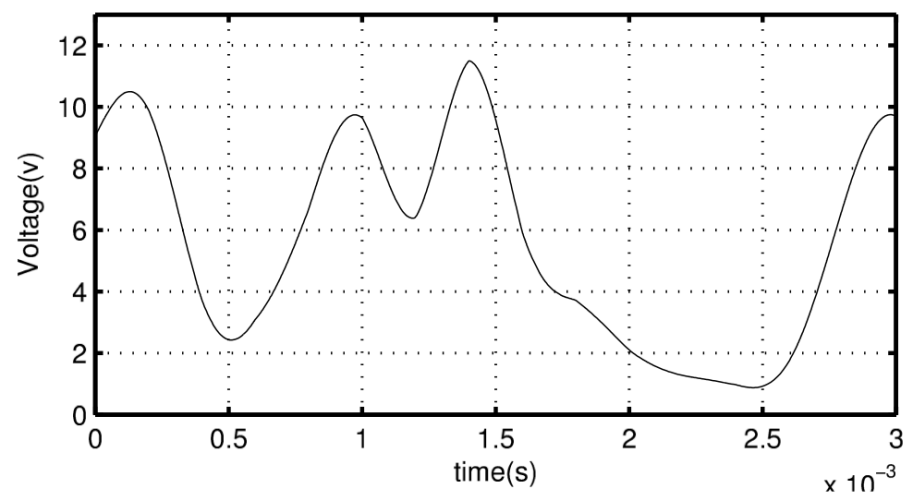
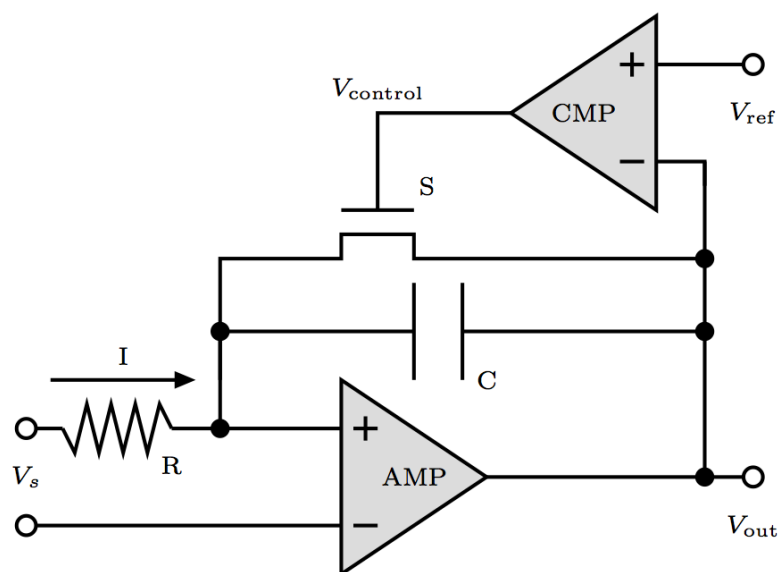


Two Types of Gaussian Decomposition

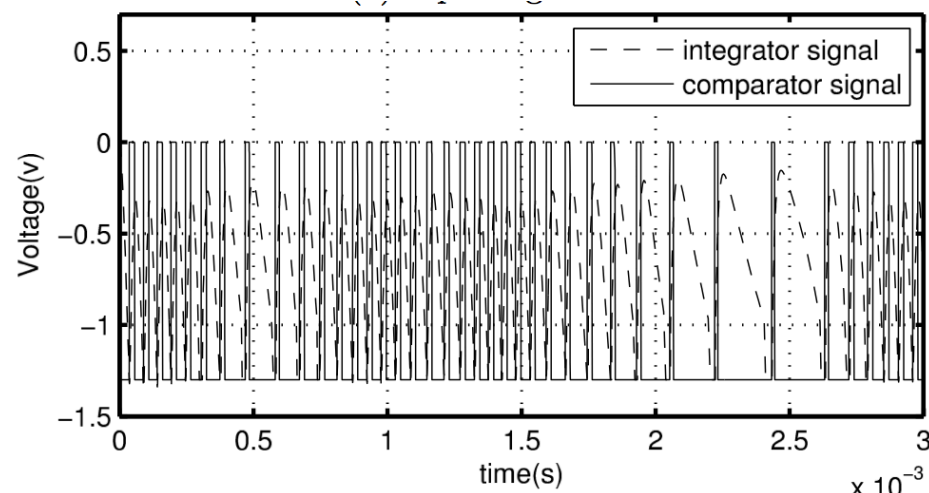


Tunable Accuracy: Number of Gaussian Components

# Gaussian Decomposition: Analog Way



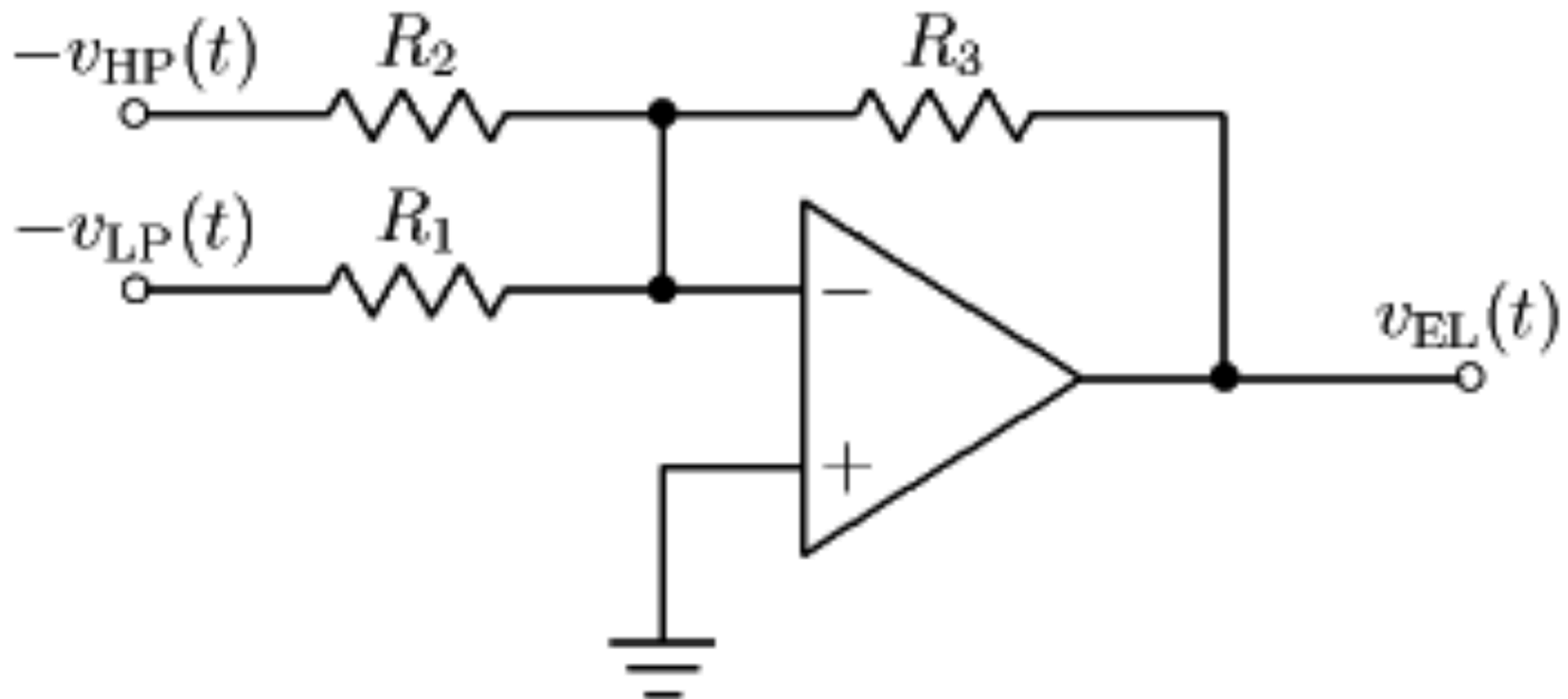
(a) Input signal.



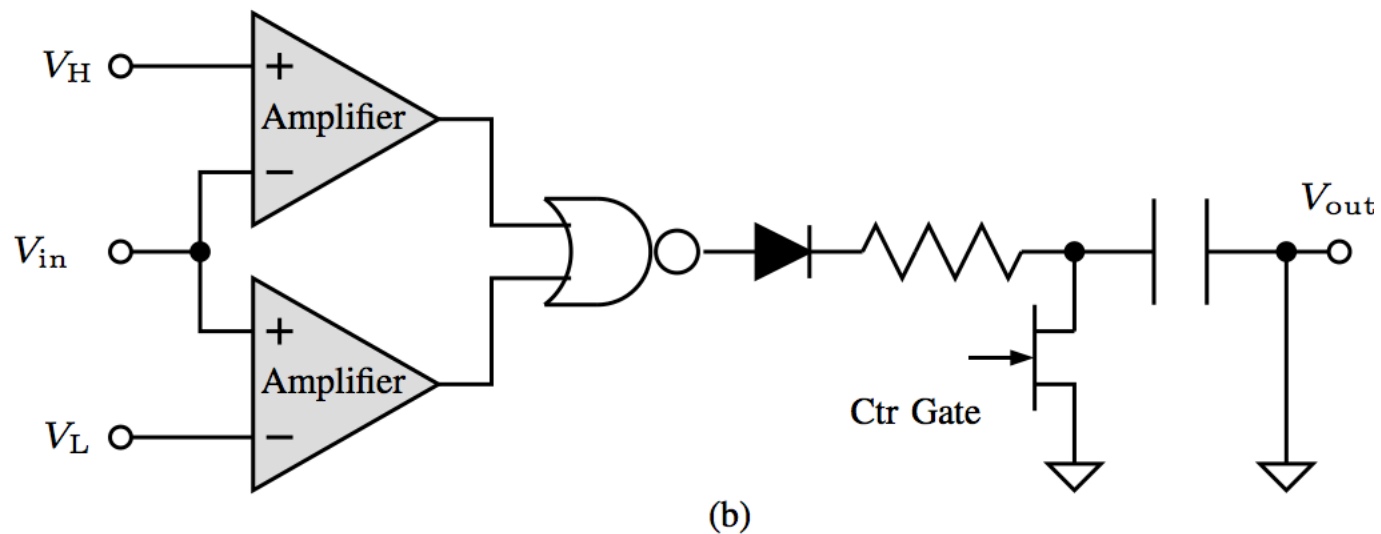
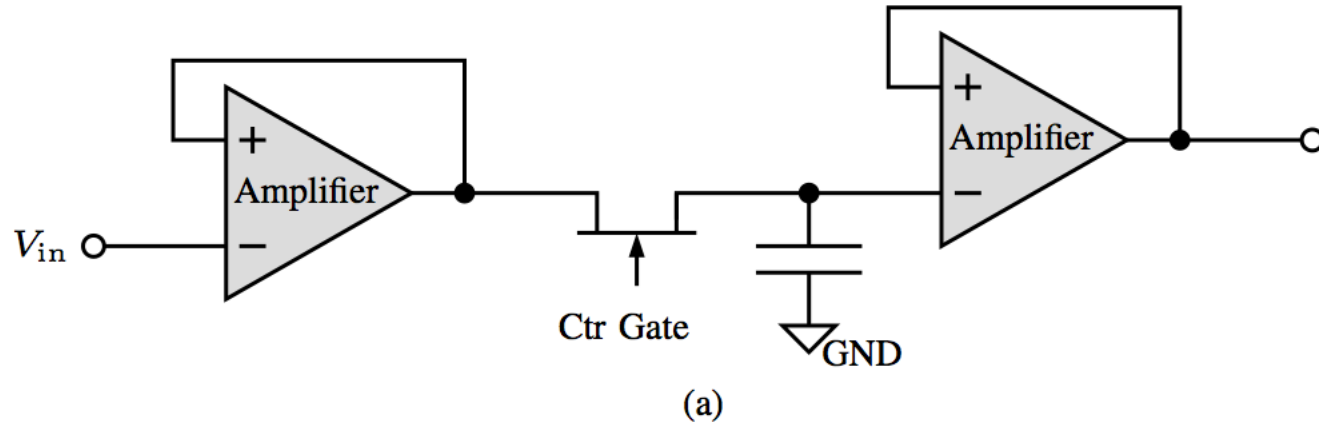
(b) Gaussian decomposition response.

# Analog Adder

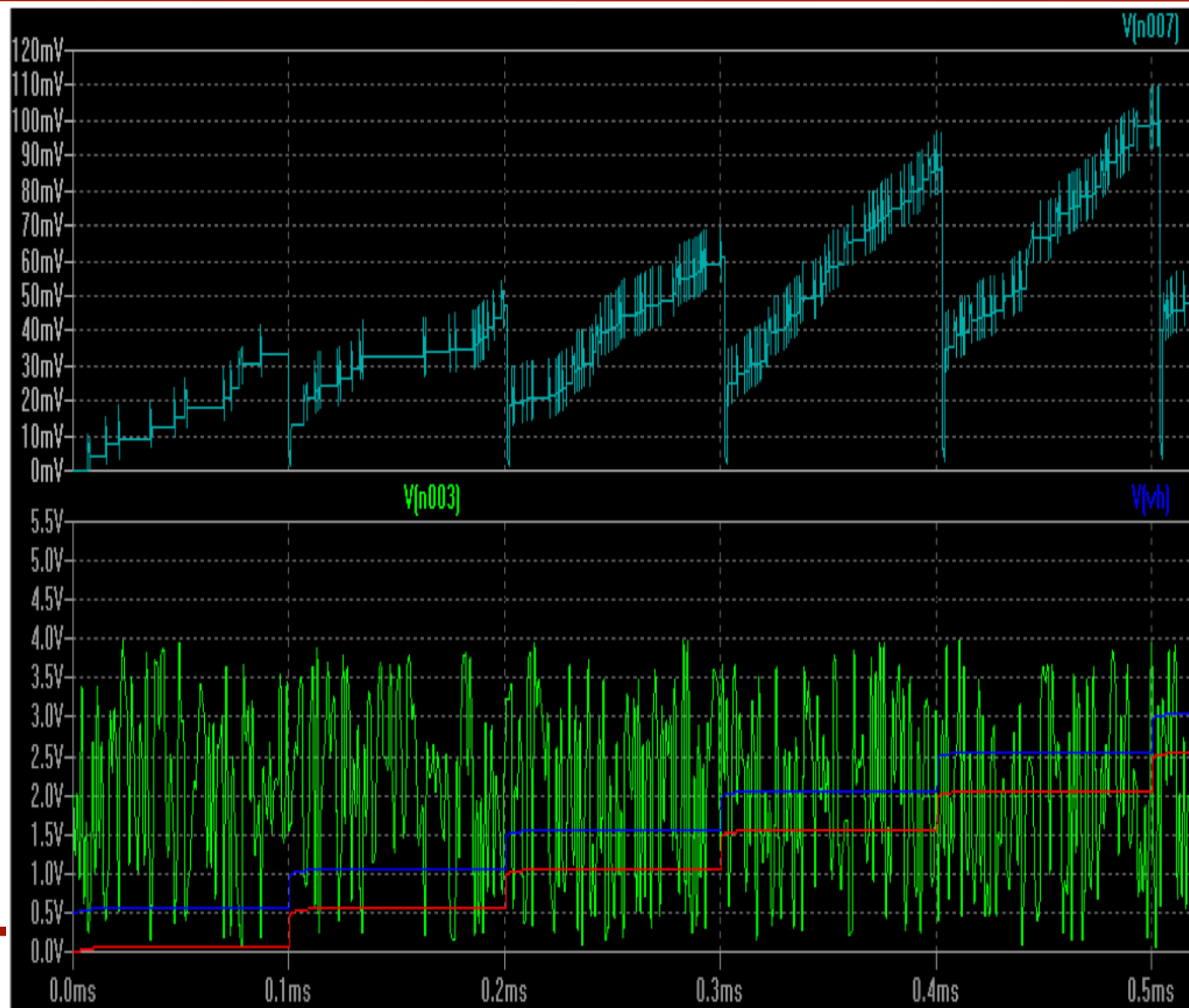
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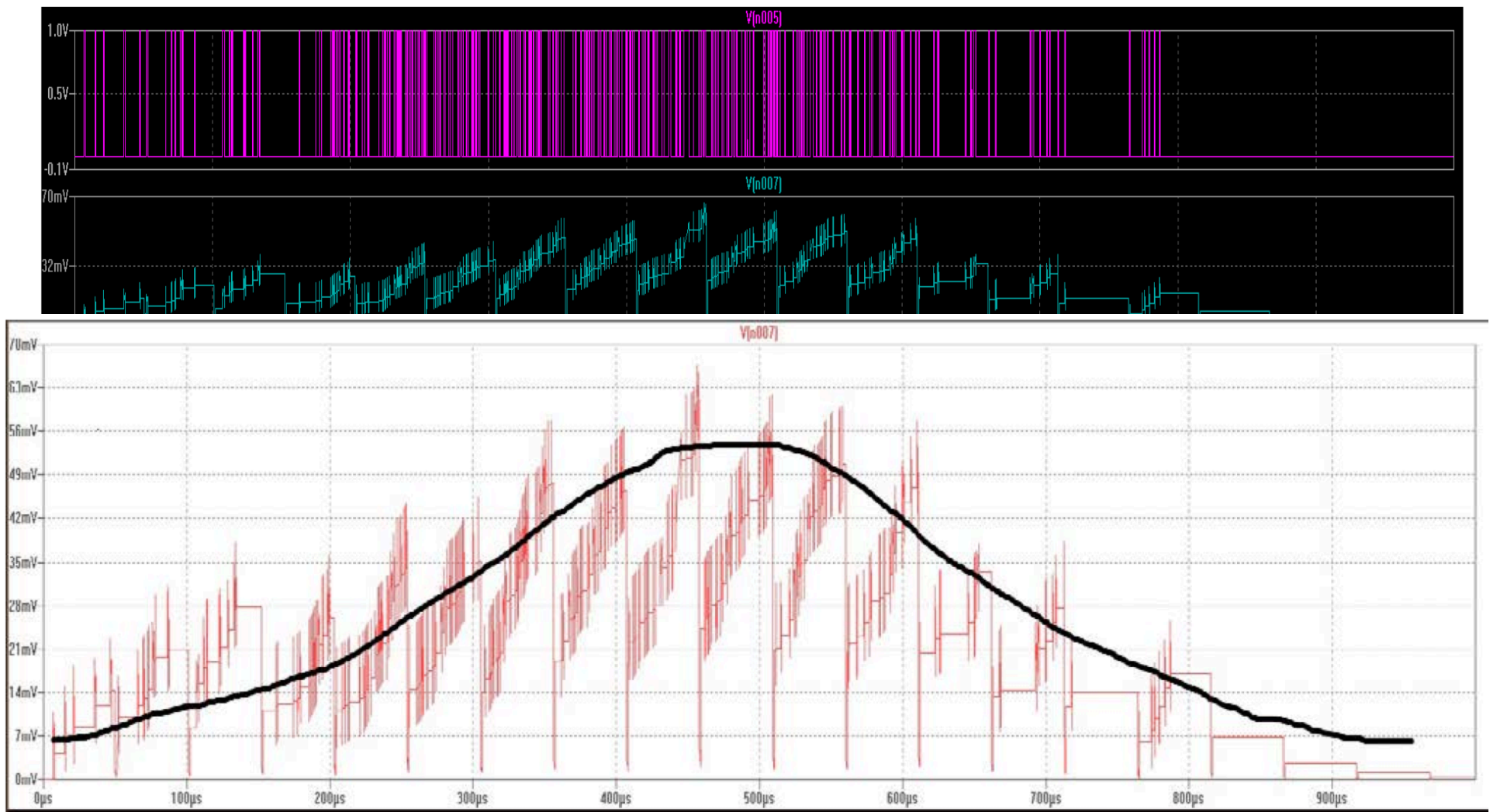
# Random Samples → PDF: Analog Way



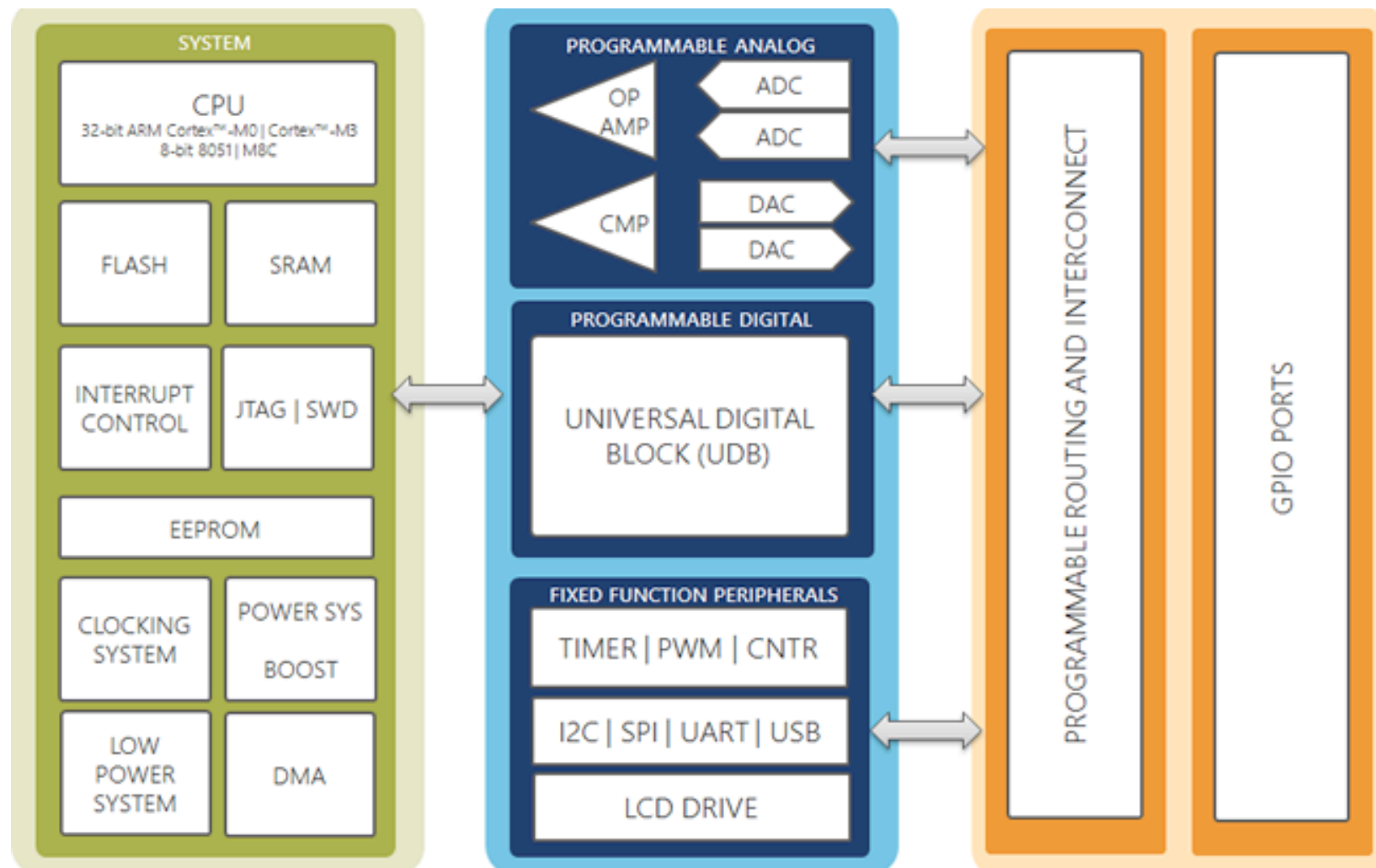
# Random Samples → PDF: Results



# Random Samples → PDF: Results

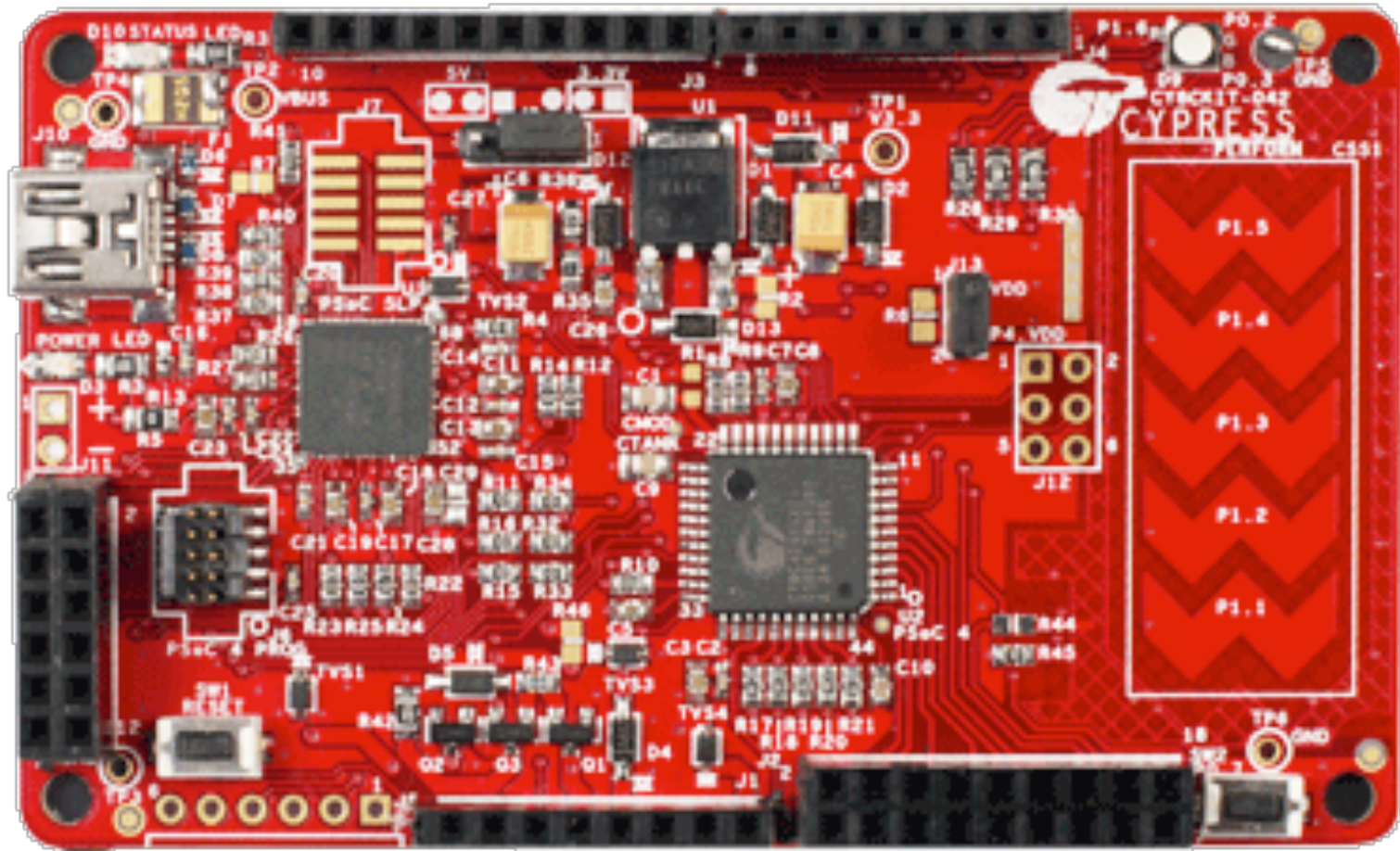


# PSoC Platform for Implementation



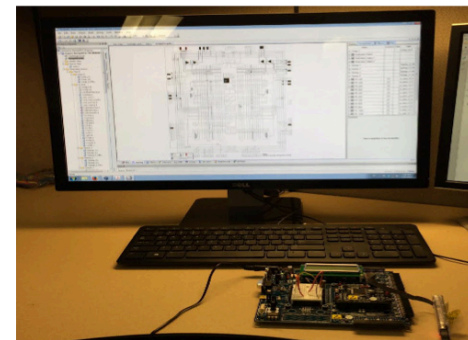
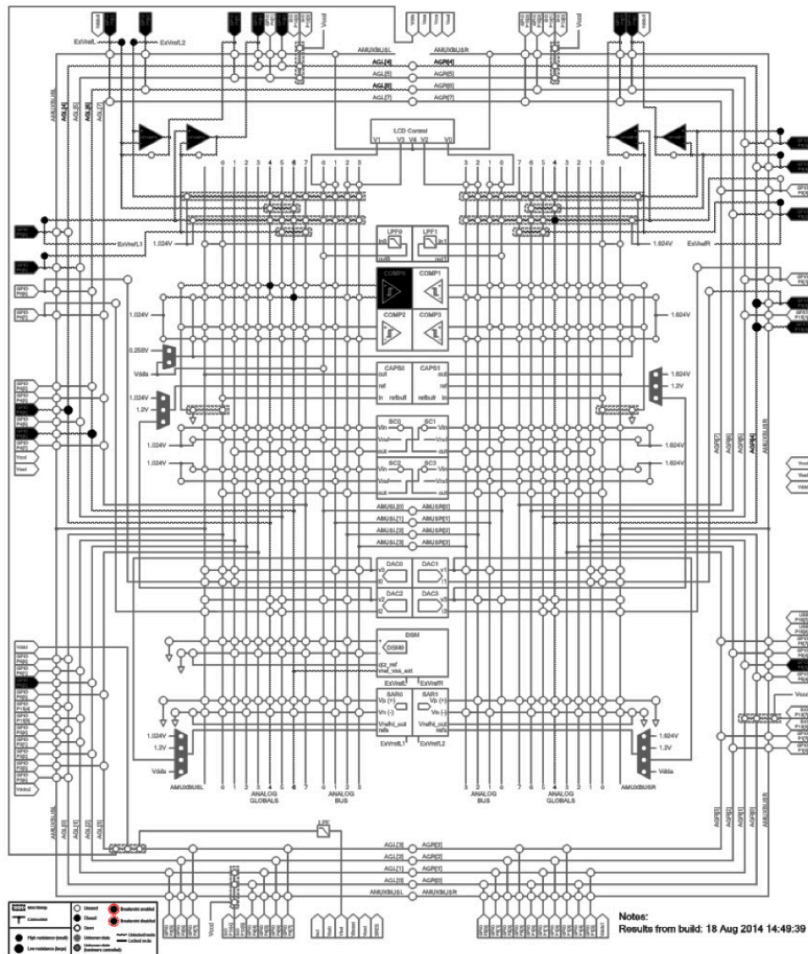


# PSoC Board

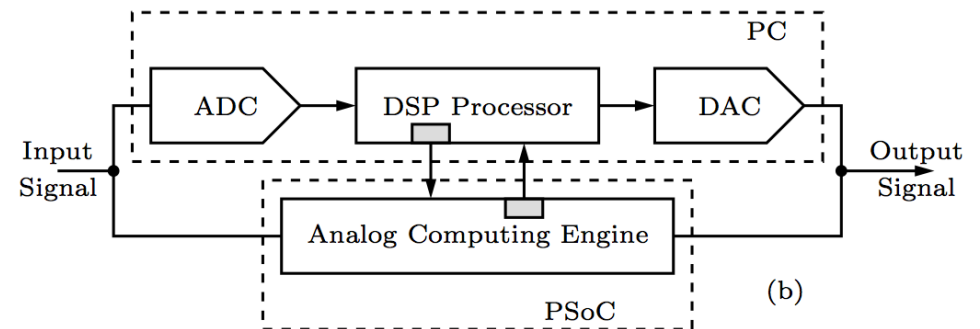




# PSoC System Implementation



(a)



(b)

# Hardware Usage and Energy Consumption

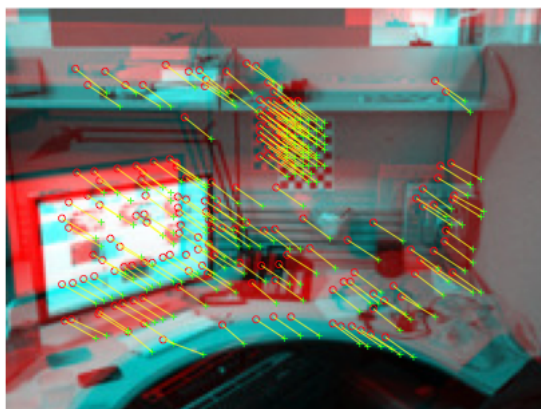
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		FPGA-Based			PSoC-Based		
		64	1024	4096	64	1024	4096
Area	Slice LUT	950	3308	13232			
	Slice Registers	426	1436	5744			
	Slice	310	1036	4144			
	Opamp				4	6	8
	comparator				1	1	1
	capacitor				4	8	12
	resistor				5	9	14
	diode transistor				4	7	13
Power	Dynamic Power (mW)	107.82	137.87	186.28	46.66	55.29	64.88
	Energy Consumption (nJ)	1196.80	1098.82	830.81	427.24	392.43	153.86

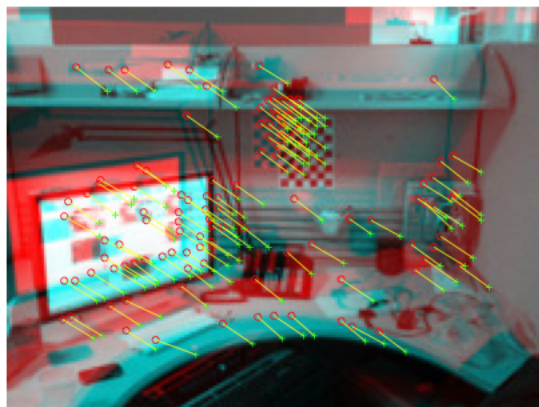
~1/3 of Dynamic Power, ~1/6 of Total Energy Consumption at 99% accuracy

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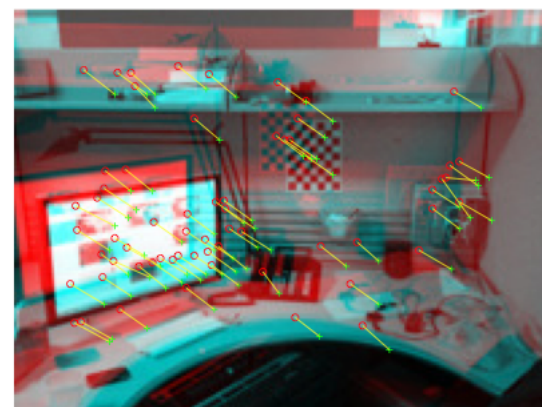
# App1: *Finding Corresponding Features*



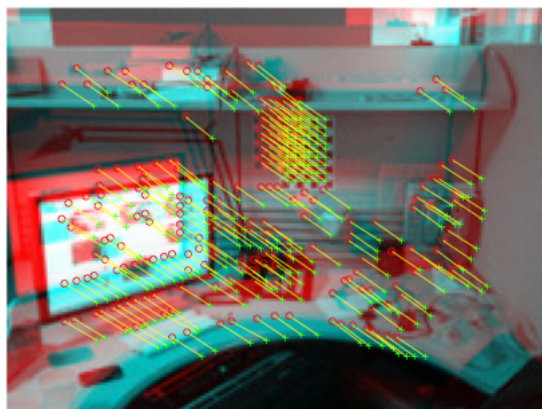
(a)  $\sigma=1\%$ ,  $P = 185$ .



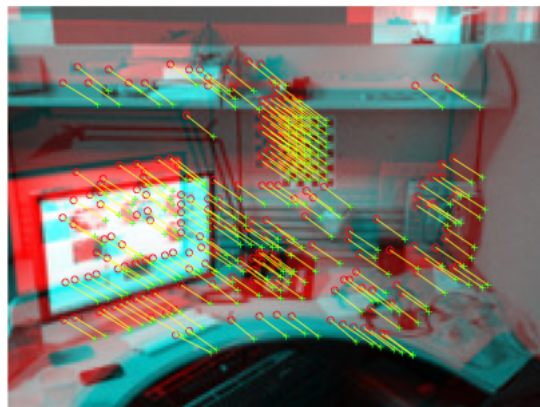
(c)  $\sigma=5\%$ ,  $P = 114$ .



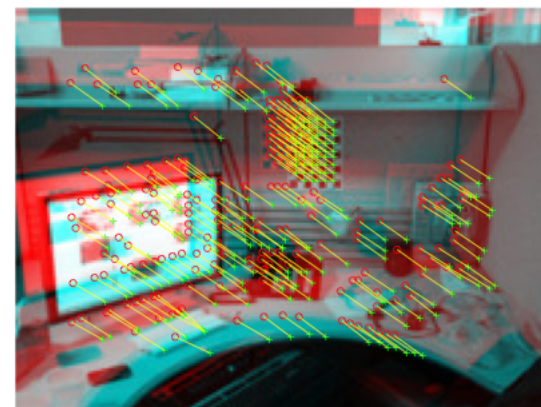
(e)  $\sigma=10\%$ ,  $P = 60$ .



(b)  $\sigma=1\%$ ,  $P = 234$ .



(d)  $\sigma=5\%$ ,  $P = 230$ .



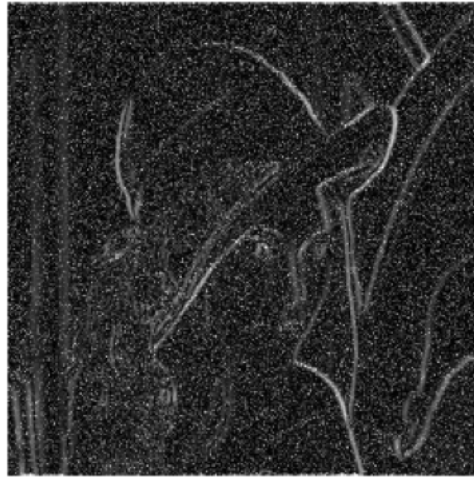
(f)  $\sigma=10\%$ ,  $P = 220$ .



## App2: Convolution-Based Edge Detection



(a)  $\sigma=1\%$ .



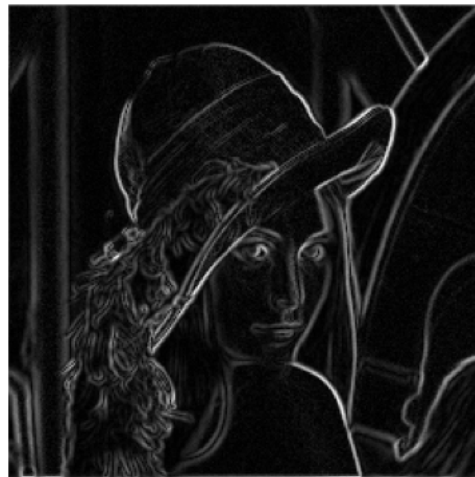
(c)  $\sigma=5\%$ .



(e)  $\sigma=10\%$ .



(b)  $\sigma=1\%$ .



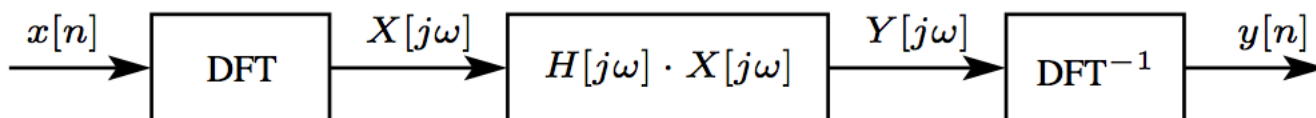
(d)  $\sigma=5\%$ .



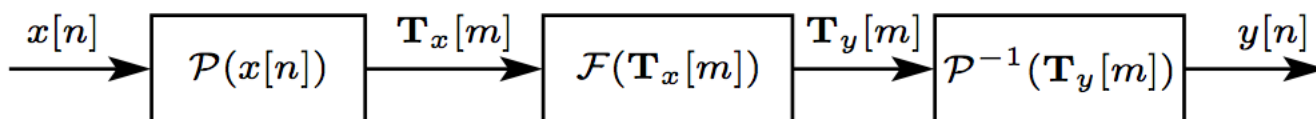
(f)  $\sigma=10\%$ .

# Question 1: How Versatile?

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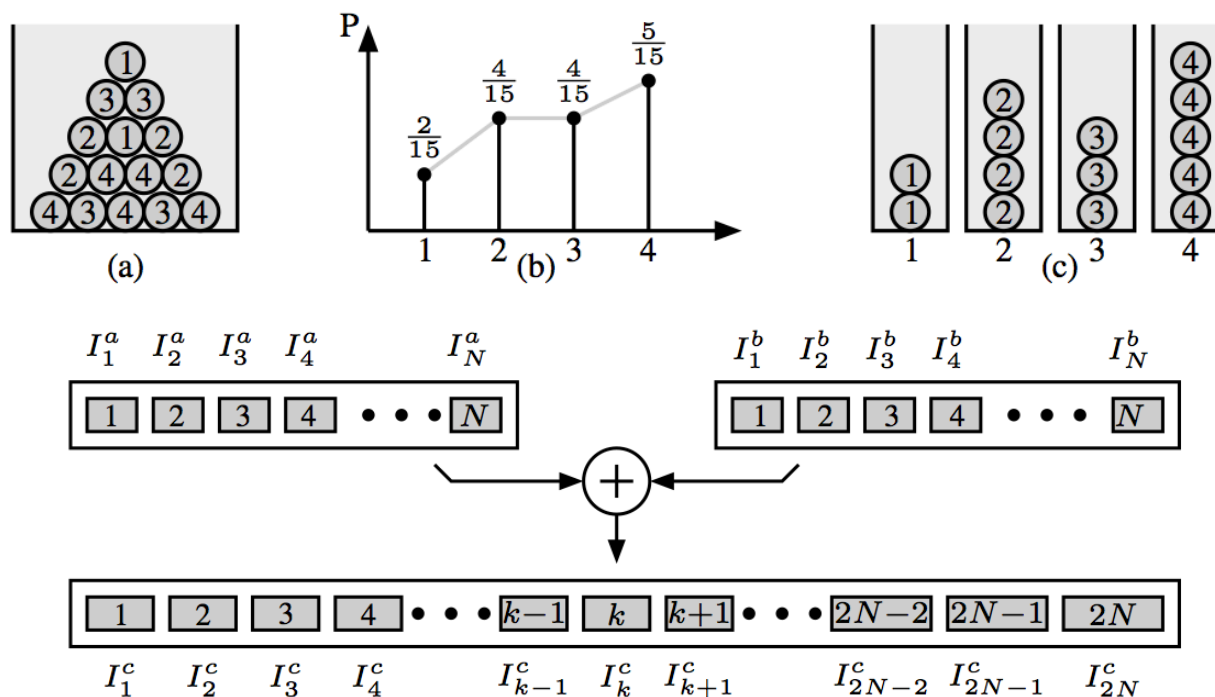


(a)



- Computing Framework: Probabilistic Domain Transform
- Perception-Based Computing Tasks
  - Convolution-Like Applications: FIR, Correlation, ...
  - Associative Computing, ...

## Question 2: How Accurate?



$$\Pr(|W_i^c - S \times q_k| \geq \delta \times S \times q_k) < \exp\left(-\frac{\delta^2 \cdot S}{N}\right).$$

Chernoff Bound  $\rightarrow$  # Random Samples vs. Accuracy

# Thanks! Questions?

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